## Optimization Methods in Science and Engineering

#### Juan Meza

High Performance Computing Research Lawrence Berkeley National Laboratory <u>http://crd.lbl.gov/~meza</u>

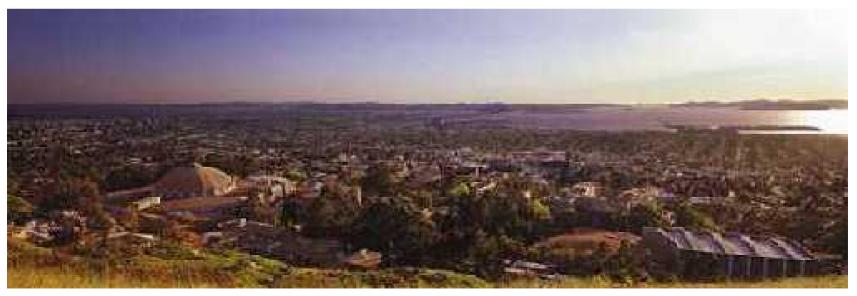


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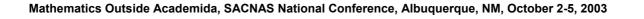


## Lawrence Berkeley National Laboratory

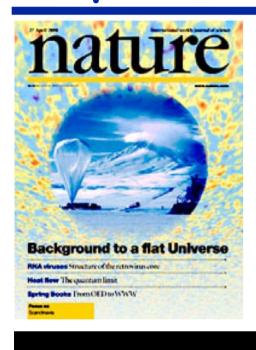
- Department of Energy national laboratory
- Open, unclassified, basic research
- Home to NERSC, the fifth largest supercomputing center in the world (7.3 Tflops)
- Located in the hills next to University of California, Berkeley campus





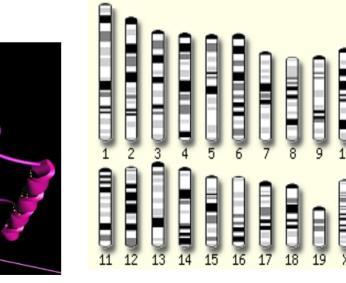


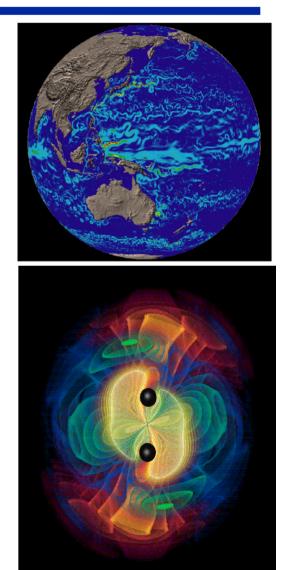
# LBNL sponsors a wide range of computational sciences activities



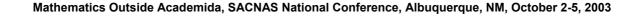






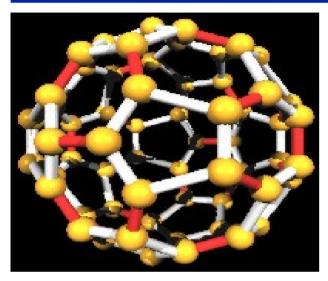


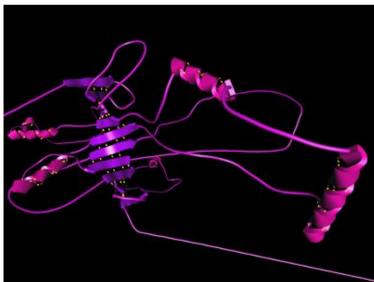






## Modeling and simulation often involves optimization





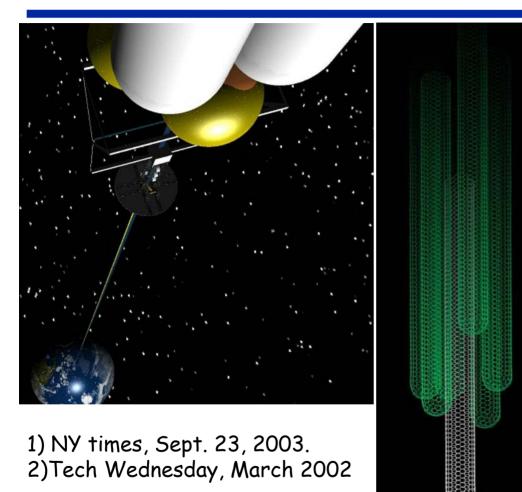
http://graphics.cs.ucdavis.edu/~okreylos/ResDev/ProtoShop/index.html

- Predict properties of nanostructures or design nanostructures with desired properties
- Protein folding problems attempt to construct 3D structures from a linear sequence (the genome)
- These simulation-based optimization problems have different characteristics than standard problems



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## World's tallest elevator!

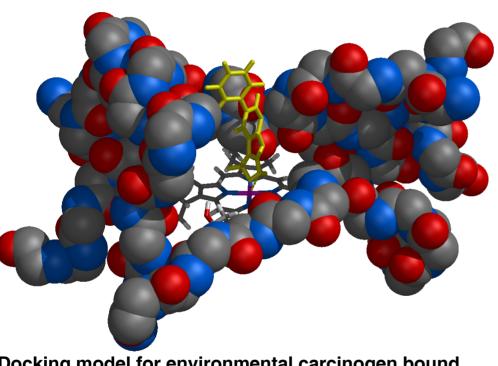


Idea is to build an elevator 60,000 miles high to carry cargo into space Concept is based on designing ultrastrong fiber strands from carbon nanotubes These ribbons of nanotubes would be woven into one paper-thin meterwide ribbon





## Molecular structure prediction



Docking model for environmental carcinogen bound in *Pseudomonas Putida* cytochrome P450

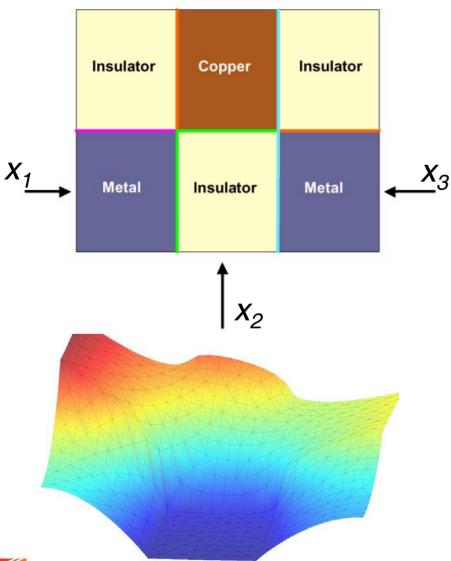
A single new drug may cost over \$500 million to develop and the design process typically takes more than 10 years

- There are thousands of parameters and constraints
- There are thousands of local minima

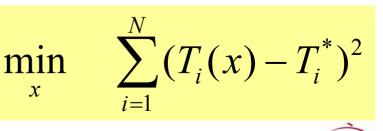




## Parameter identification



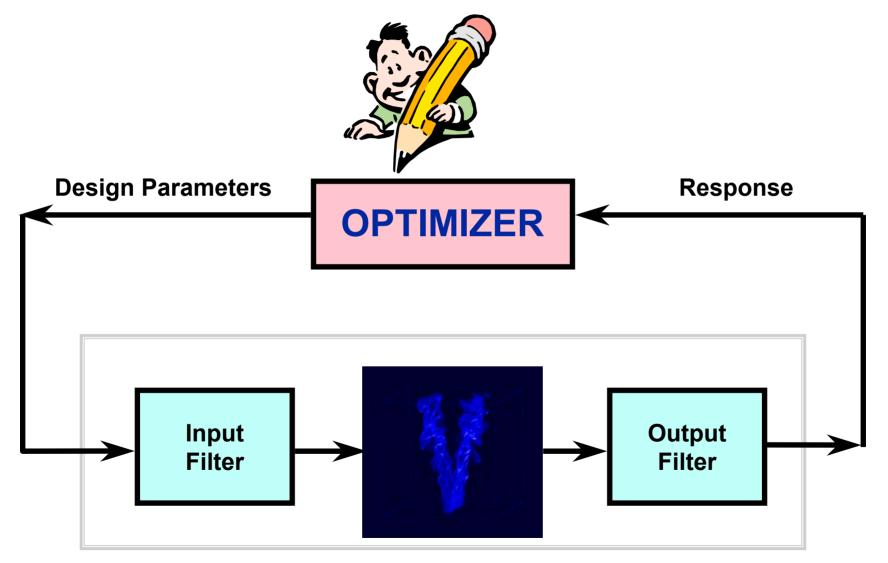
- Find model parameters, (satisfying some bounds), for which the simulation matches the observed temperature profiles
- Objective function consists of computing the temperature difference between simulation results and experimental data:





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## Optimization can be used in conjunction with simulation codes







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## **General Optimization Problem**

 $\min_{x\in\mathfrak{R}^n}f(x),$ 

## s.t. h(x) = 0, $g(x) \ge 0$

**Objective function** 

Equality constraints

Inequality constraints





## **Optimization Problem Types**

- Unconstrained optimization
- Bound constrained optimization
  - Only upper and lower bounds
  - Sometimes called "box" constraints
- General nonlinearly constrained optimization
  - Equality and inequality constraints
  - Usually nonlinear
- Some special case classes
  - Linear programming (function and constraints linear)
  - Quadratic programming (quadratic function, linear constraints)





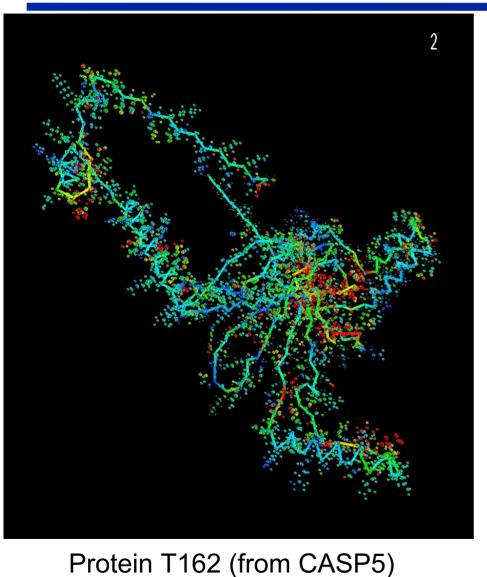
# Why are simulation-based optimization problems different?

- Objective function is smooth
  - Usually true, but simulations can create noisy behavior
- Twice continuously differentiable
  - Usually true, but difficult to prove
- Constraints are linearly independent or hard
  - Users can sometimes over-specify or incorrectly guess constraints
  - Require strict feasibility
- Expensive objective functions
  - Dominant cost is evaluation of function





#### Energy Minimization Using Limited Memory BFGS (LBFGS)



Energy Function: AMBER
Protein 162;
N = 13728 (4576 Atoms)
LBFGS with M=15

- Total number of LBFGS iterations = 11656
- Total number of function evaluations = 11887
- Each function evaluation takes approximately 5 CPU sec





### **Amber Function**

$$\begin{split} E_{AMBER} &= E_{Bonds} + E_{Angles} + E_{Dihedrals} + E_{NonBonded} \\ E_{Bonds} &= \sum_{Bonds} K_{r_i} (r_i - \overline{r_i})^2 \\ E_{Angles} &= \sum_{Angles} K_{\theta_i} \left( \theta_i - \overline{\theta_i} \right)^2 \\ E_{Dihedrals} &= \sum_{Dihedrals} K_{\phi_i} \left( 1 + \cos(n_i \phi_i - \delta_i) \right) \\ E_{NonBonded} &= \sum_{i} \sum_{i < j} \left( \varepsilon_{ij} \left[ \left( \frac{\sigma_{ij}}{r_{ij}} \right)^{12} - 2 \left( \frac{\sigma_{ij}}{r_{ij}} \right)^6 \right] + \frac{q_i q_j}{r_{ij}} \right) \end{split}$$

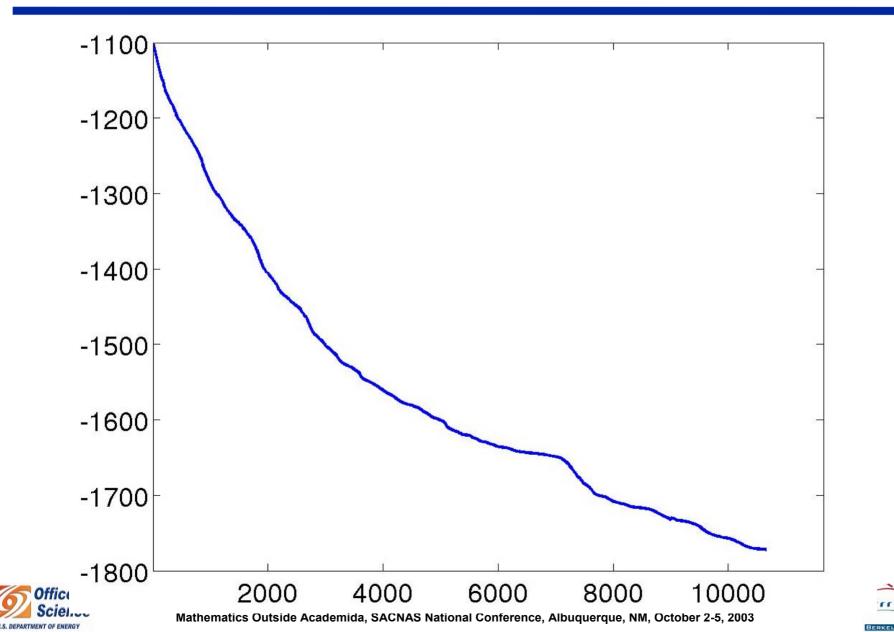
A Physical Approach to Protein Structure Prediction, Crivelli, et.al. Biophysical Journal, Vol 82, 2002.





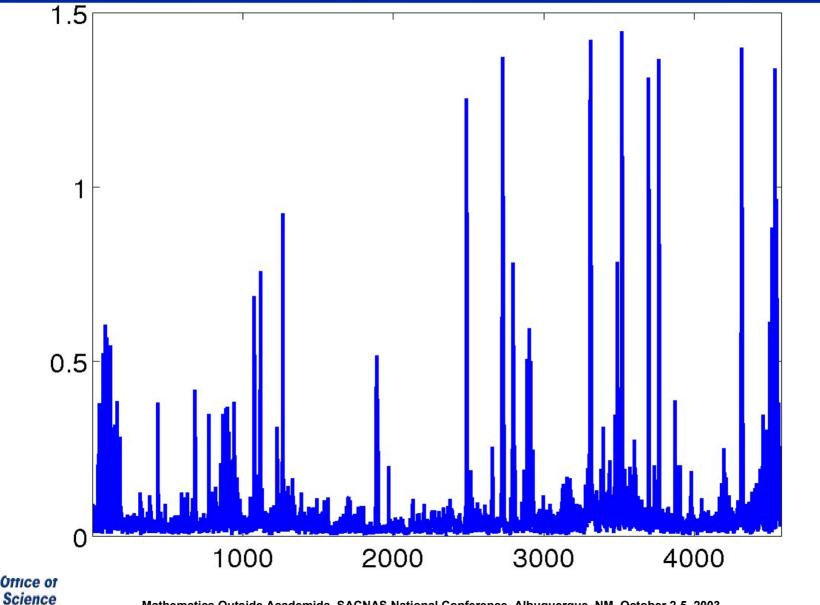
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#### Energy vs. LBFGS iterations for T162 Problem



rrrr

## T162 Protein: ||gradient|| by atom



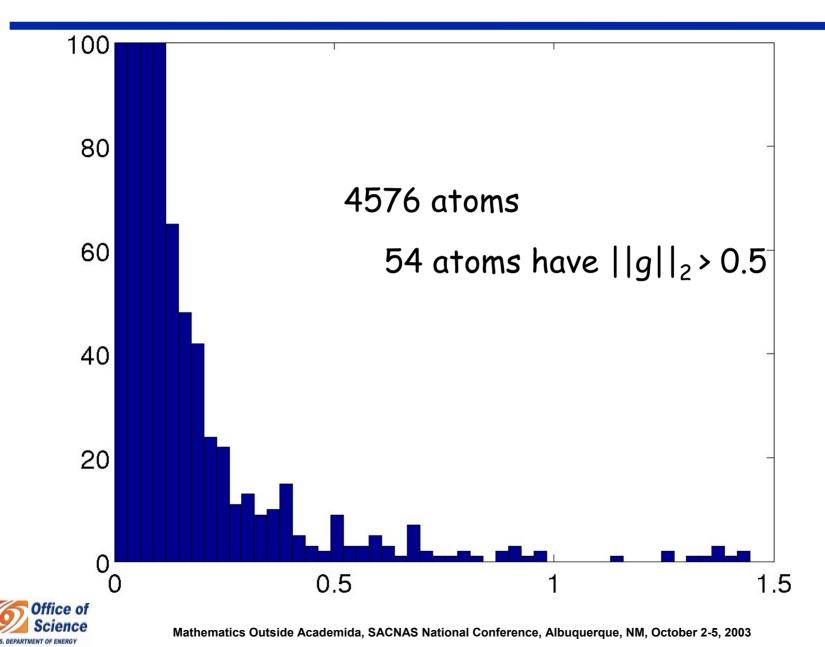


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BERKELEY

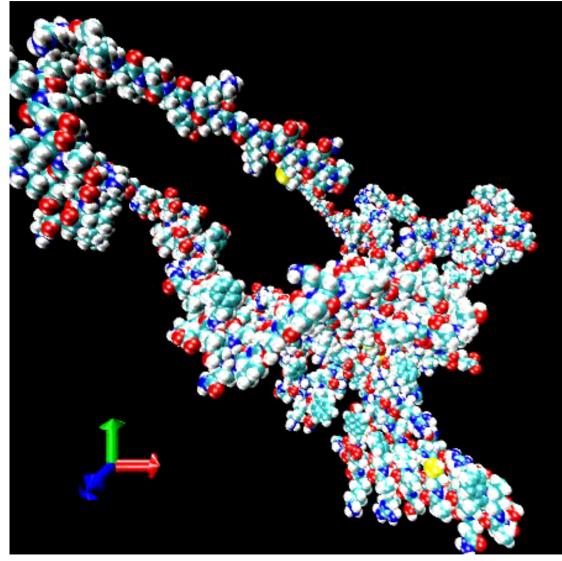
## Distribution of ||gradient|| by atom



rrrr

BERKEL

## Protein T162 (from CASP5)



- Initial configuration created using ProteinShop (S. Crivelli)
- Energy minimization computed using OPT++/LBFGS
- Final average RMSD change was 3.9 Å
- Total simulation took approximately 32 hours on a 1.7GHz machine





#### Summary

- Wide range of scientific and engineering problems requiring mathematics
- Many of these scientific and engineering problems involve nonlinear optimization problems
- Thorough knowledge of both science and mathematics is required to address these problems - the solution of these problems requires interdisciplinary teams, creativity, and a little bit of luck.









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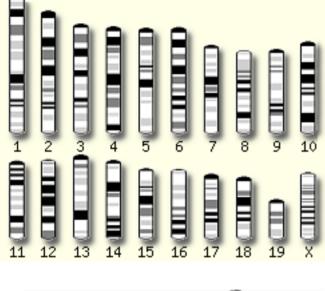
## **Backup Slides**



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## JAZZ Genome Assembler







Assembly of Fugu genome from 3.1 million reads, and initial preparation of mouse genome data.

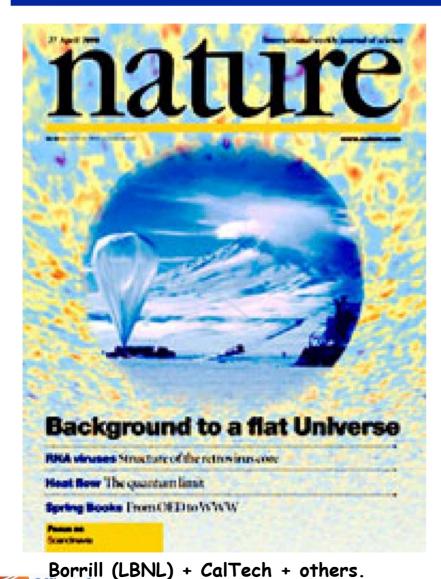
#### NERSC provided:

- porting of JAZZ assembler, BLAST alignment tool, cross\_match alignment tool, and MySQL client to the IBM SP
- a dedicated MySQL server
- resolved issues installing a MySQL server on the IBM SP
- consulting support for parallelization of BLAST and cross\_match tool
- Dan Rokhsar, Joint Genome Institute





#### Analyzing Cosmic Microwave Background Radiation

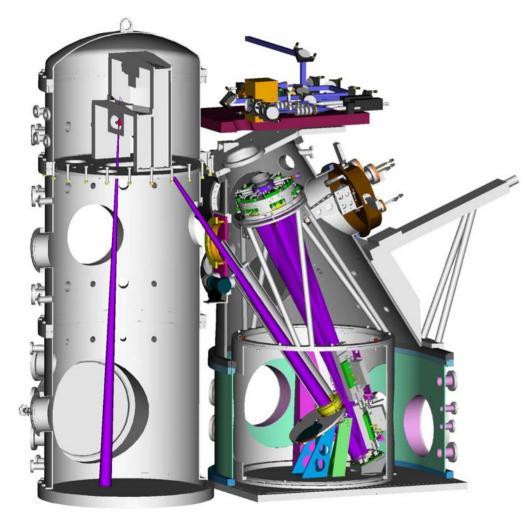


- BOOMERANG Experiments analyze cosmic microwave background radiation data to obtain a better understanding of the universe
- The data analysis provides strong evidence that the geometry of the universe is flat
- Computational capability provided on NERSC platforms
- MADCAP software developed at NERSC for general community



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## Parameter identification example



- Find model parameters, satisfying some bounds, for which the simulation matches the observed temperature profiles
- Computing objective function requires running thermal analysis code
- Each simulation
   requires approximately
   7 hours on 1 processor



