

Derivative-Free Optimization Methods for the Surface Structure Determination Problem

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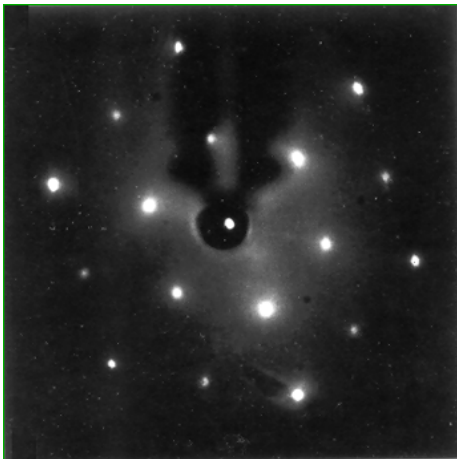
Acknowledgements

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Surface structure determination

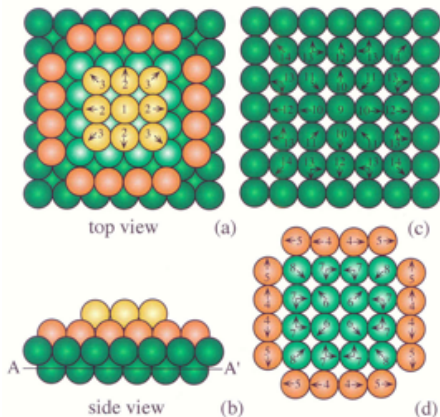
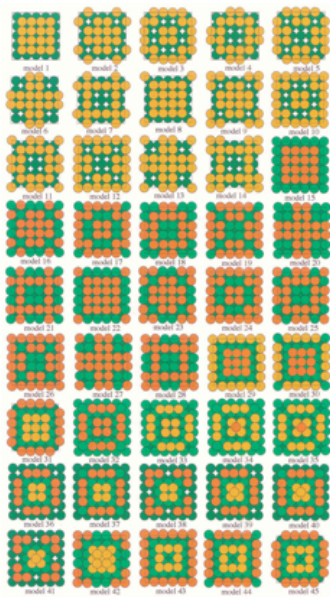
- Surface structure determines many important properties of materials.
- Possibility of electron diffraction first proposed by deBroglie (1924).
- Over 40 years before it became a tool in surface structure determination.
- Low-energy electrons are surface sensitive, requiring a well-ordered surface.
- Experimental data could not be quantitatively described by kinematic theory and necessitated the development of a theory of multiple scattering in the late 1960s.

Low-energy electron diffraction (LEED)



- Goal is to determine surface structure through low energy electron diffraction (LEED).
- Need to determine the coordinates and chemical identity of each atom: Li atoms on a Ni surface
- Non-structural parameters, i.e. inner potential, phase shift δ , thermal effects and damping.
- www.answers.com/topic/low-energy-electron-diffraction

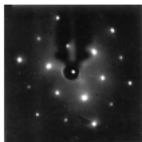
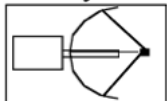
Surface structure determination using LEED



LEED setup

Experiment

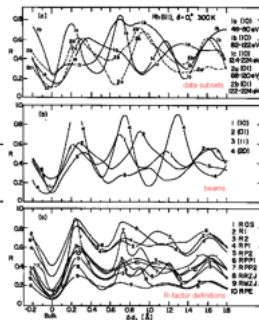
LEED system



I-V spectra



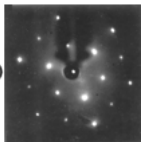
R-Factors



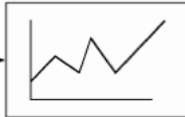
Theory

(x,y,z) input parameters

- 1) (-1.33, -0.08, 2.51)
- 2) (0.33, 0.00, 0.00)
- 3) (1.89, 1.22, 3.51)



I-V spectra



Pendry R-factor

- Pendry R(eliability) -factor (1980) is defined by:

$$R = \sum_{i,g} (Y_{gth} - Y_{gexp})^2 / \sum_{i,g} (Y_{gth}^2 + Y_{gexp}^2)$$

$$Y(E) = L / (1 + LV_{oi}^2),$$

$$L(E) = I' / I,$$

$$L \approx \sum_j \frac{-2(E - E_j)}{(E - E_j)^2 + V_{oi}^2}$$

- LEED curves consist for the main part of a series of Lorentzian peaks:
 $I \approx \sum a_j / (E - E_j)^2 + V_{oi}^2$
- Their widths are dictated by the imaginary part of the electron self-energy (optical potential): $\Delta E = 2|V_{oi}|$
- Pendry R-factor emphasizes positions of the maximum and minimum rather than the heights of the intensities
- Ideal agreement corresponds to $R = 0$; uncorrelated spectra yields $R = 1$.

Optimization formulation

- Inverse problem
 - minimize R-factor - defined as the misfit between theory and experiment
 - Several ways of computing the R-factor, we will use the Pendry R-factor.
- Combination of continuous and categorical variables
 - Atomic coordinates: x , y , z
 - Chemical identity: Ni, Li
- No derivatives available; function may also be discontinuous
- Invalid (unphysical) structures lead to function being undefined in certain regions and returning special values

Previous Work

- Early attempts used Hooke-Jeeves, nonlinear least squares, genetic algorithms¹⁻²,
 - We have also used pattern search methods
 - Effective, but expensive
 - Several 100 to 1000s of function calls typically needed
 - Each function call can take up to 2 minutes on a workstation class computer
-
- ① Global Optimization in LEED Structure Determination Using Genetic Algorithms, R. Dill and M.A. Van Hove, Surf. Sci. 355, L393-8 (1996).
 - ② G. S. Stone, MS dissertation, Computer Science Dept., San Francisco State University, 1998.

General MVP algorithm

Initialization: Given values Δ_0, x_0, M_0, P_0 ,

```
1   For  $k = 0, \dots, \text{maxit}$  do
2       Search: Evaluate  $f$  on a finite subset of trial points on the mesh  $M_k$ 
3       Poll: Evaluate  $f$  on the frame  $P_k$ .
4       If (successful)
5            $x_{k+1} = x_k + \Delta_k d_k$ 
6           Update  $\Delta_k$ 
7   End
```

- Global Search phase can include user heuristics or surrogate functions
- Local Poll phase is more rigid, but needed to ensure convergence.

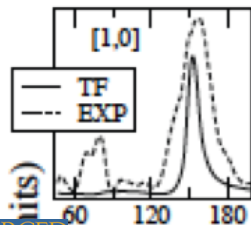
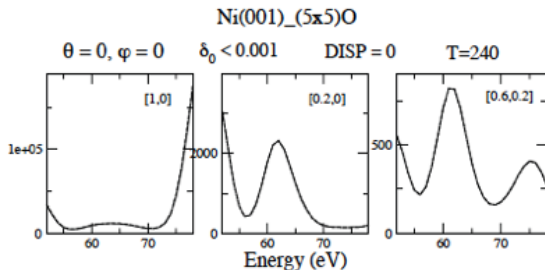
Variations on LEED

- LEED
 - Multiple scattering model
 - I-V spectra computed repeatedly until best-fit structure is found
 - Computation time is proportional to the number of parameters
- TLEED (Tensor LEED)
 - For a reference structure use multiple scattering
 - Perturbation method to calculate I-V for a structure close to a reference structure
 - Efficient for local modifications (i.e. no categorical variables) - otherwise computationally expensive

Kinematic LEED as a simplified physics surrogate (SPS)

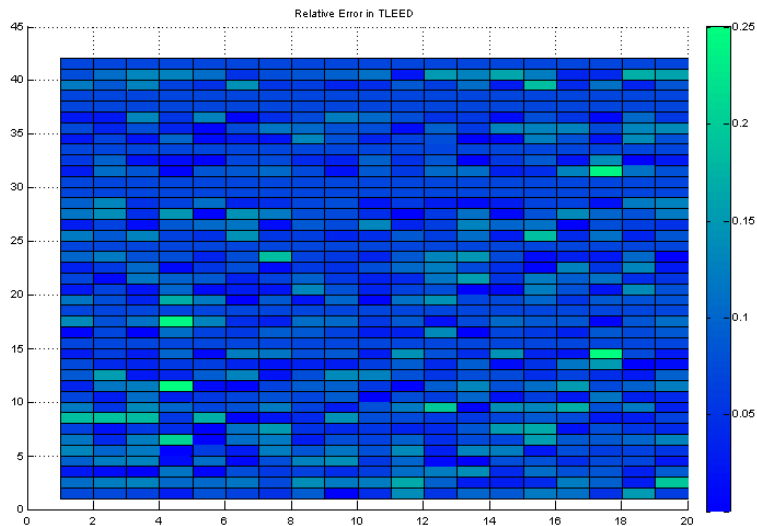
- R-factor depends on:
 - Structural parameters, i.e. atomic positions, chemical identity
 - Non-structural parameters, i.e. inner potential, phase shift δ , thermal effects and damping.
- KLEED (Kinematic LEED)
 - Basic assumption is that electrons are only scattered once by the surface atoms.
 - Surface unit cell size and symmetry can be determined, but not the exact positions of atoms
 - I-V spectra from KLEED can be computed in a few seconds compared to multiple scattering which takes ≈ 2 minutes to compute

KLEED versus TLEED(multiple-scattering)



- KLEED agrees well with experimental data as long as the incident angle is close to perpendicular
- KLEED and multiple scattering agree well with small phase shift, i.e. as $\delta \rightarrow 0$.
- However for larger phase shift there is no guarantee of agreement

KLEED as a simplified physics surrogate



Simplified physics surrogate (SPS)

- Define $\phi_A(x) = \phi_S + \phi_I$, where

ϕ_A = Additive surrogate,

ϕ_S = Simplified physics surrogate,

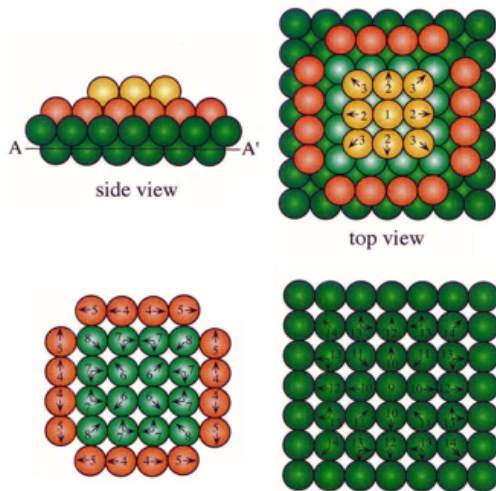
ϕ_I = Interpolatory surrogate

Search:

- 1 if (first search step) {
 - 2 Initialize ϕ_I with Latin Hypercube sample.
 - 3 else {
 - 4 recalibrate ϕ_I with DACE model of $\phi_S - f$.
 - 5 }
 - 6 Construct $\phi_A = \phi_S + \phi_I$
 - 7 Solve min ϕ_A
-

Test problem

Ni(100)-(5x5)-Li

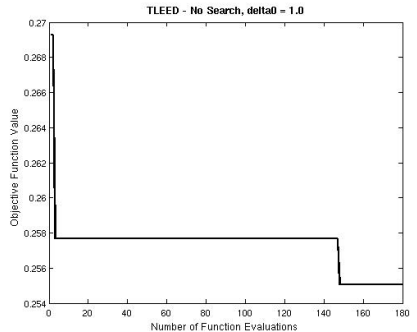
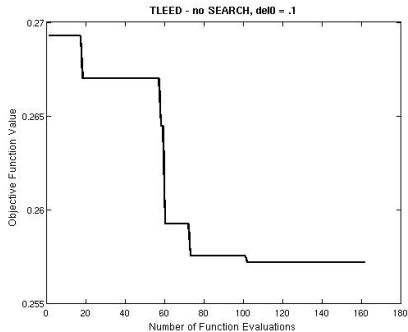


- Model 31 from set of model problem using three layers
 - 14 atoms
 - 14 categorical variables
 - 42 continuous variables
- Additional constraint added so that positions of atoms are constrained to lie within a box
- Used NOMADm, developed by M. Abramson

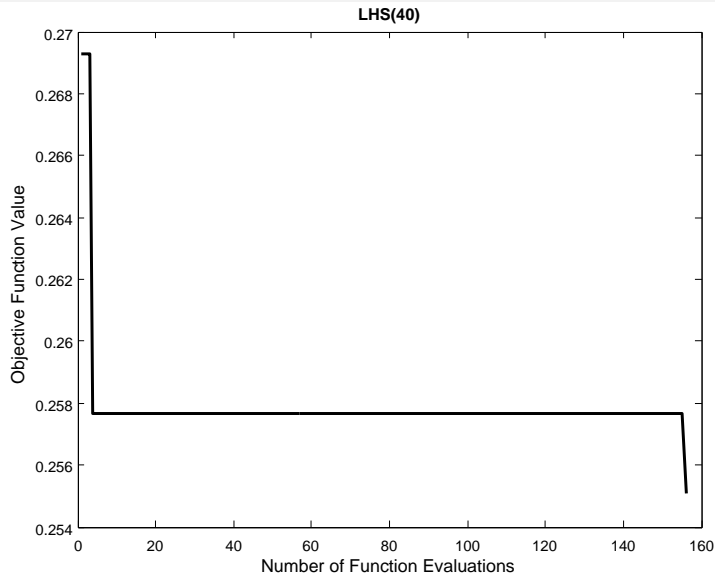
Test cases

- Start with best known feasible point
- Three different approaches
 - No search step
 - LHS search
 - Simplified physics surrogate (DACE model)
 - LHS with 5 and 15 points
 - $\Delta = 1.0$
 - $\Delta = 0.1$

Optimization of continuous variables using no search phase

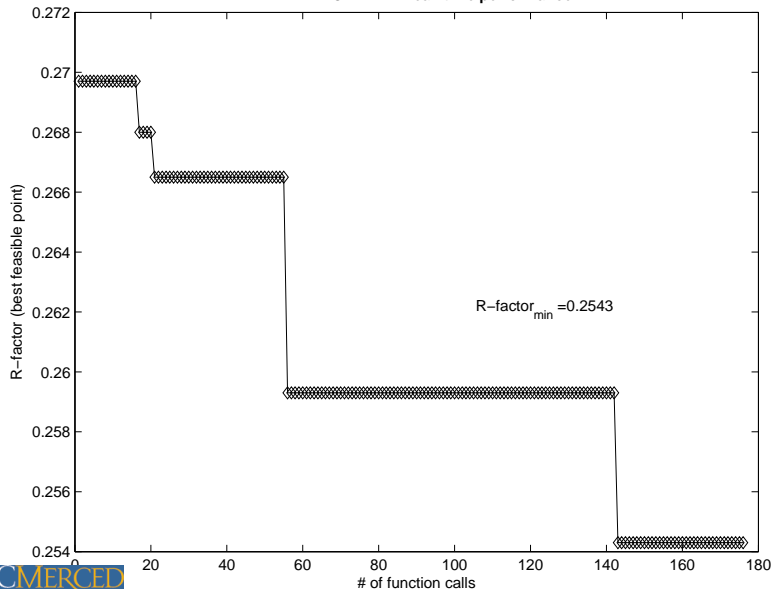


Optimization using LHS with 40 points

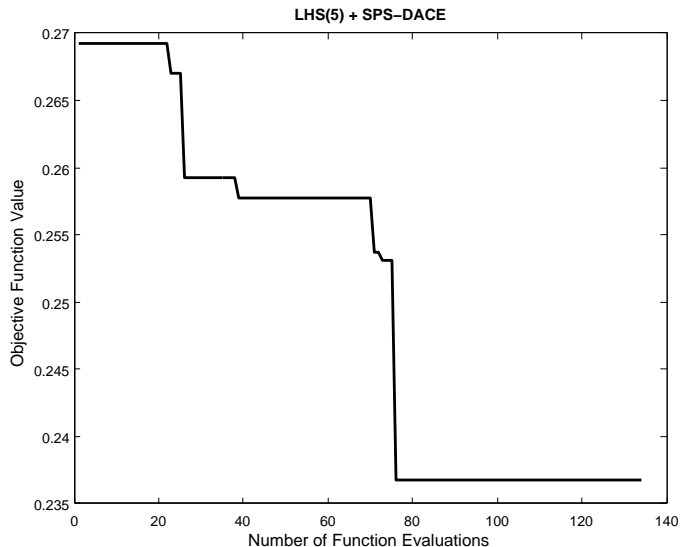


Optimization using additive surrogate, $\Delta_0 = 1.0$

TLEED-NOMADm: Real-time performance



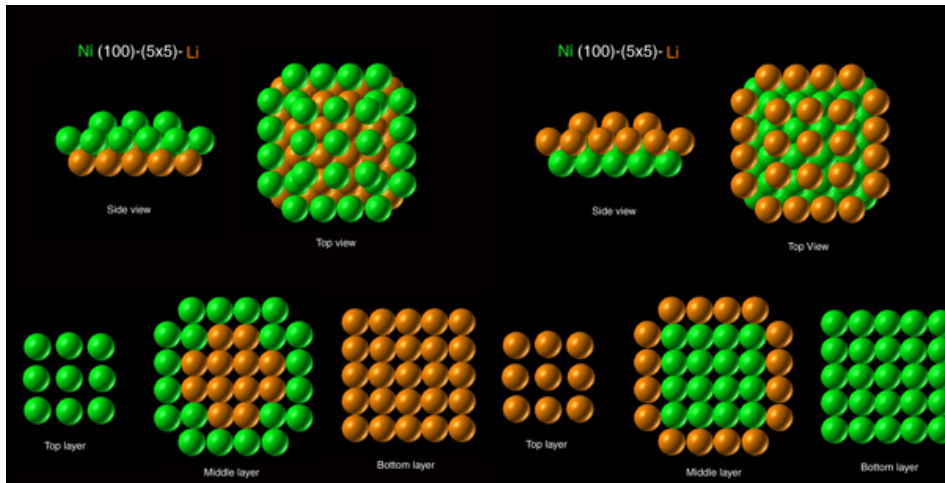
Optimization using additive surrogate, $\Delta_0 = 0.1$



Summary of numerical results

Method	LHS	$f(x^*)$	fevals
No search	0	0.2551	180
LHS	40	0.2551	160
SPS+DACE	15	0.2543	180
SPS+DACE	5	0.2354	135

LEED Chemical Identity Search: Ni (100)-(5x5)-Li



Summary

- Preliminary results indicate that performance can be enhanced by using an additive surrogate function in the search phase.
- Total number of function evaluations decreased by about 20%, which represents a reduction of ≈ 2 hours per model.
- Efficiency is (too) dependent on various algorithmic parameter.

Future Work

- Working on interfacing to new C++ version of Nomad
- Combine continuous with categorical variables
- Need to investigate alternatives to DACE model, e.g. Bayesian techniques

UC Merced is hiring



Photo by Larry Salinas